

# The optimal electrode thickness and porosity

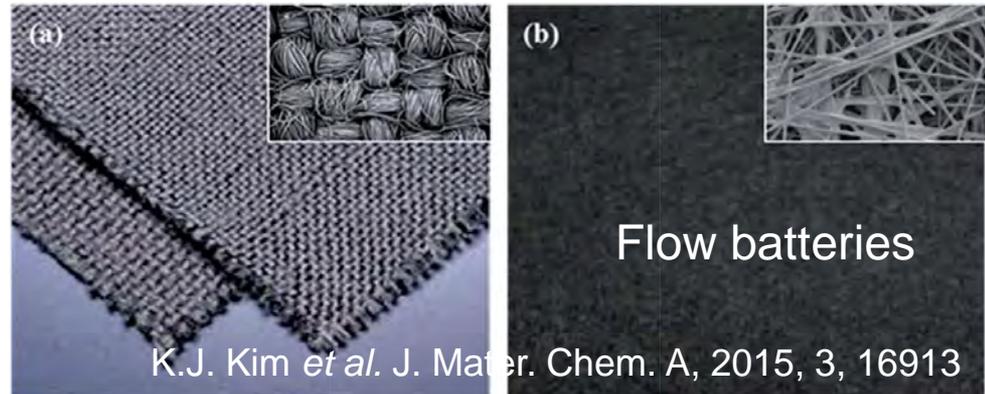
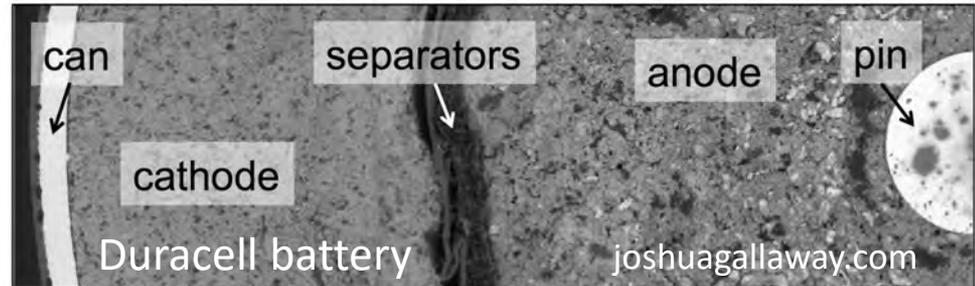
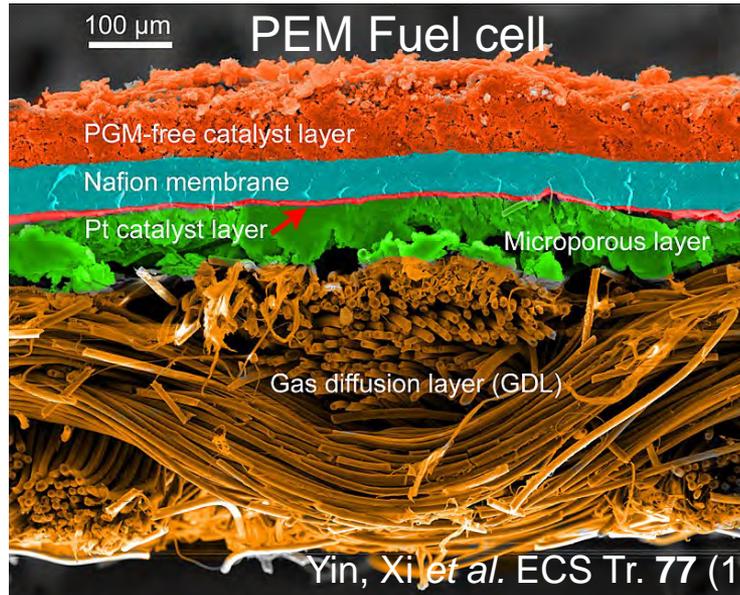
J.W. (Willem) Haverkort

Assistant Professor  
*Process & energy*

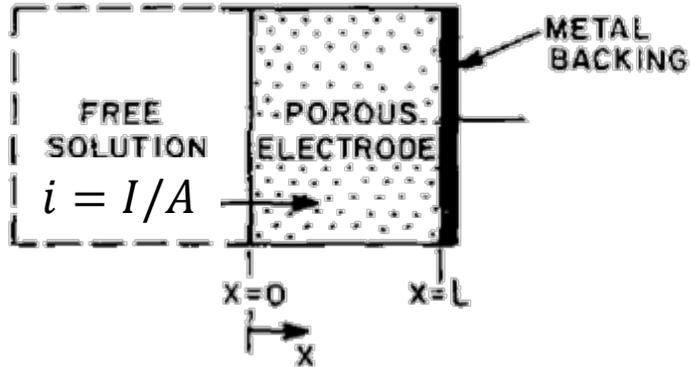


Towards sustainable production  
of chemicals and fuels

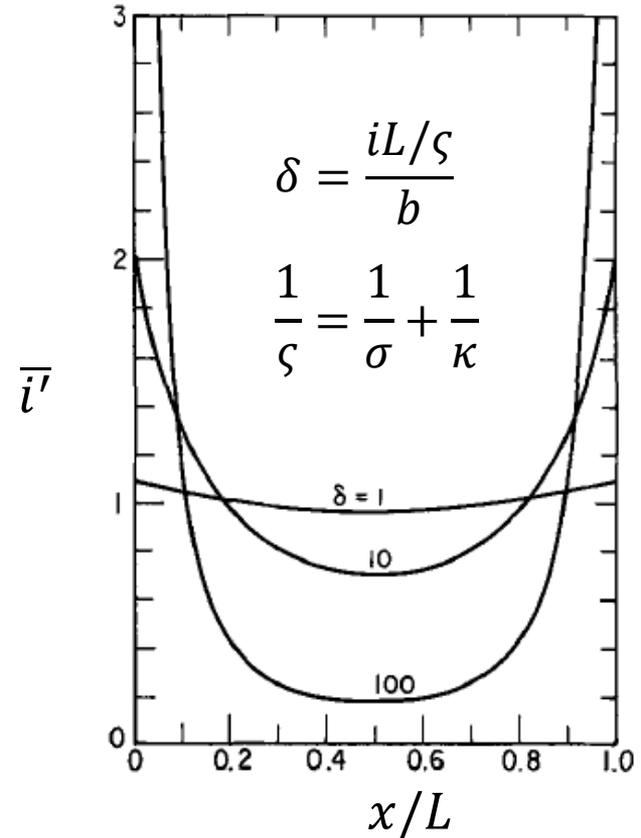
# Porous electrodes



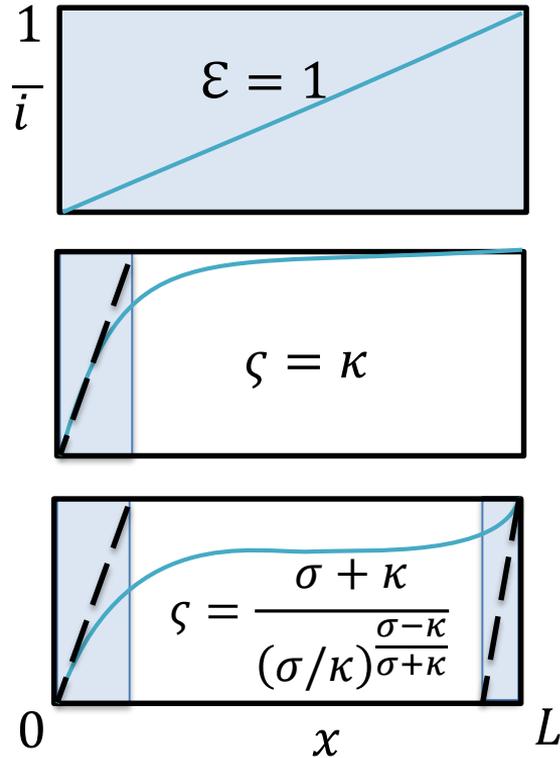
# Newman & Tobias 1962



- Constant conductivities  $\sigma, \kappa$
- Tafel slope  $b = RT/\alpha F$



# Electrode Effectiveness Factor



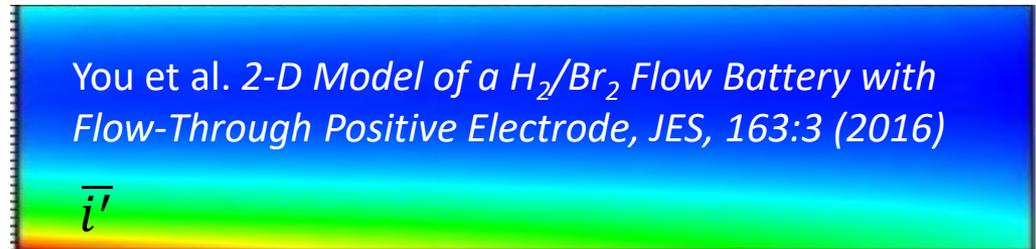
$$\Delta V = b \ln \left( \frac{i}{\epsilon i_*^{\text{tot}}} \right) + \frac{iL}{\sigma + \kappa}$$

$$i_*^{\text{tot}} = aLi_*$$

$$\epsilon \approx (1 + \mathcal{J}^p)^{-\frac{1}{p}}$$

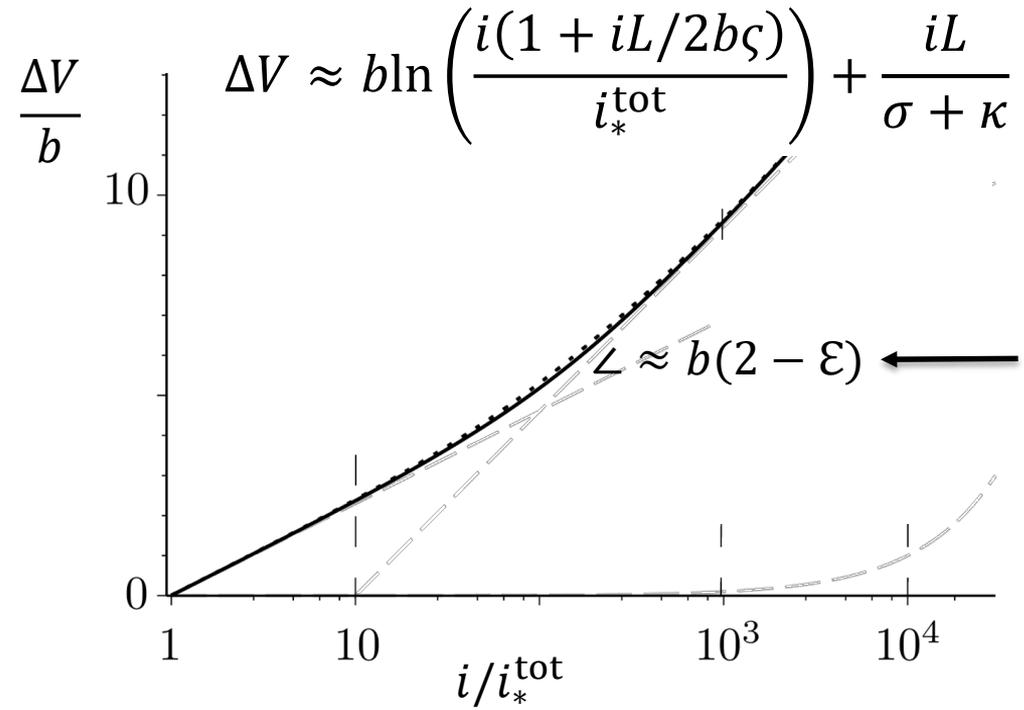
$$\mathcal{J} \sim \delta/2$$

Paulin *et al.* '77, Scott '82, Costamagna *et al.*, '98  
Catalyst utilization, e.g. Gasteiger *et al.*



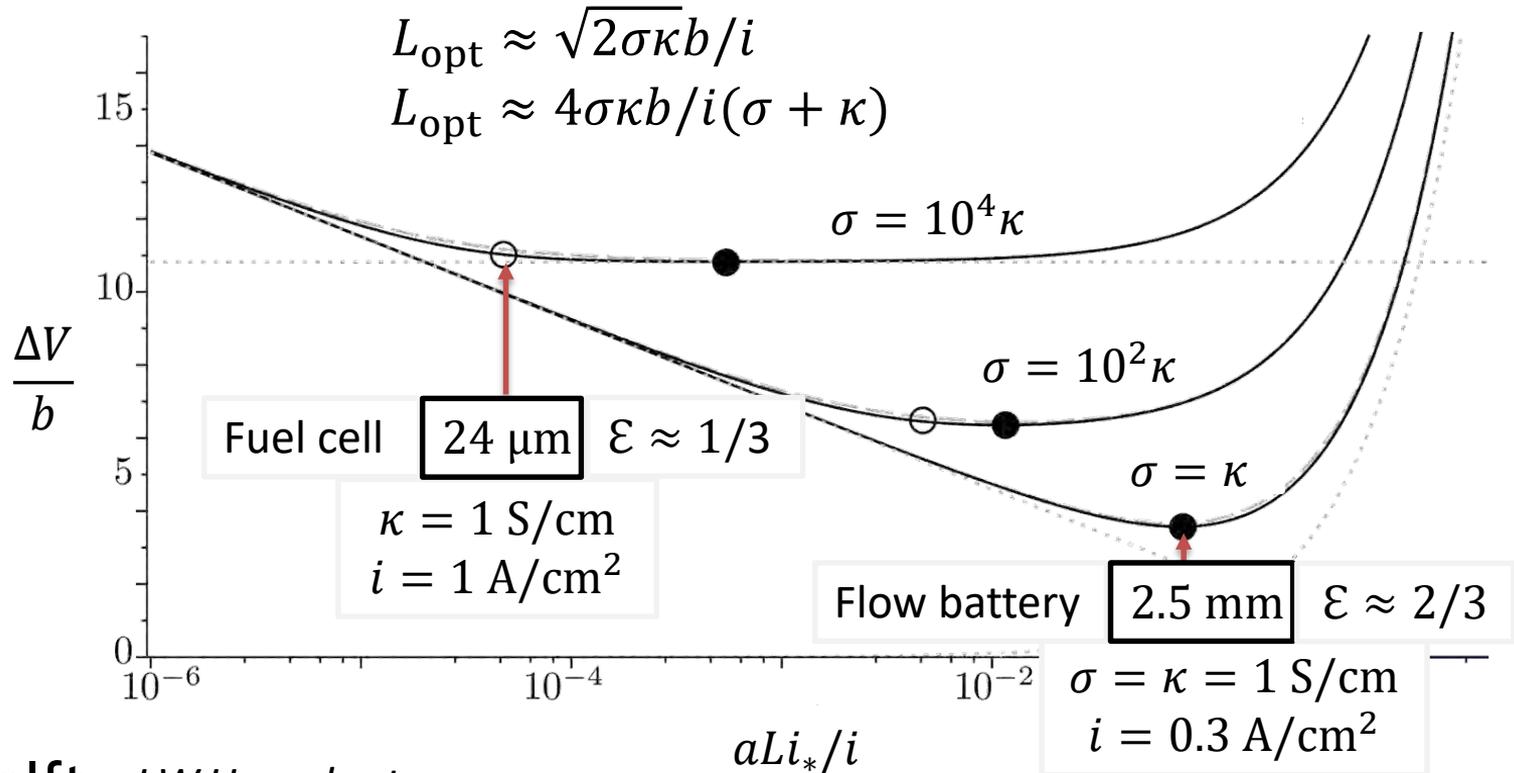


# Explicit $i - \Delta V$ relation



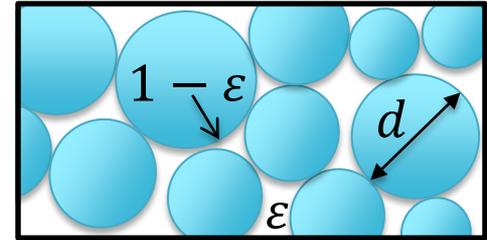
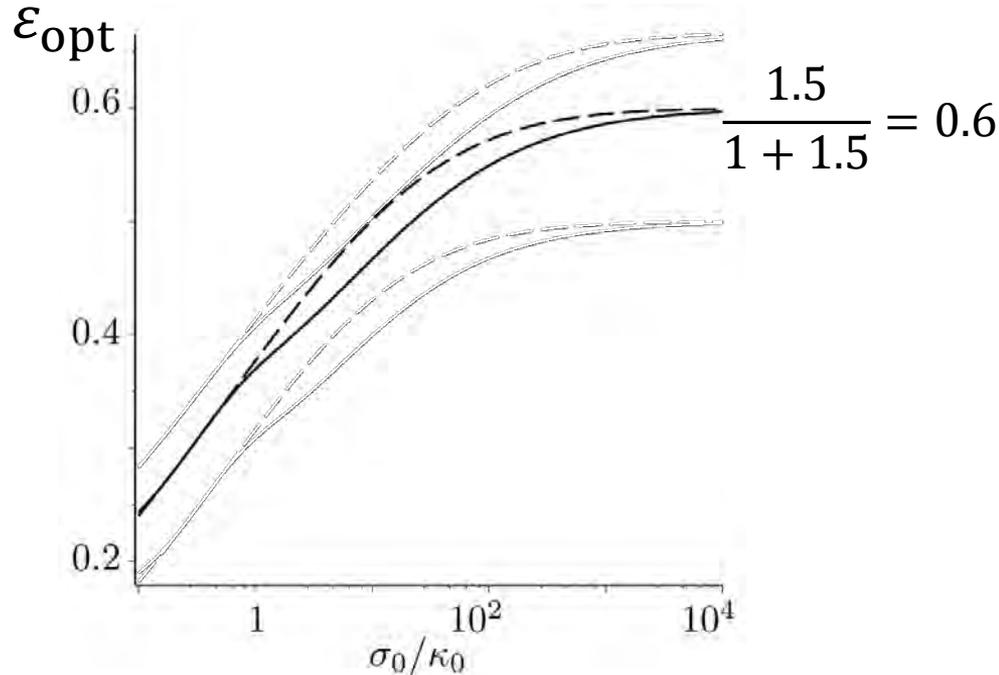
*Tafel slope doubling*  
Austin, Eikerling,  
Kulikovsky, Soderberg,...

# Optimal electrode thickness



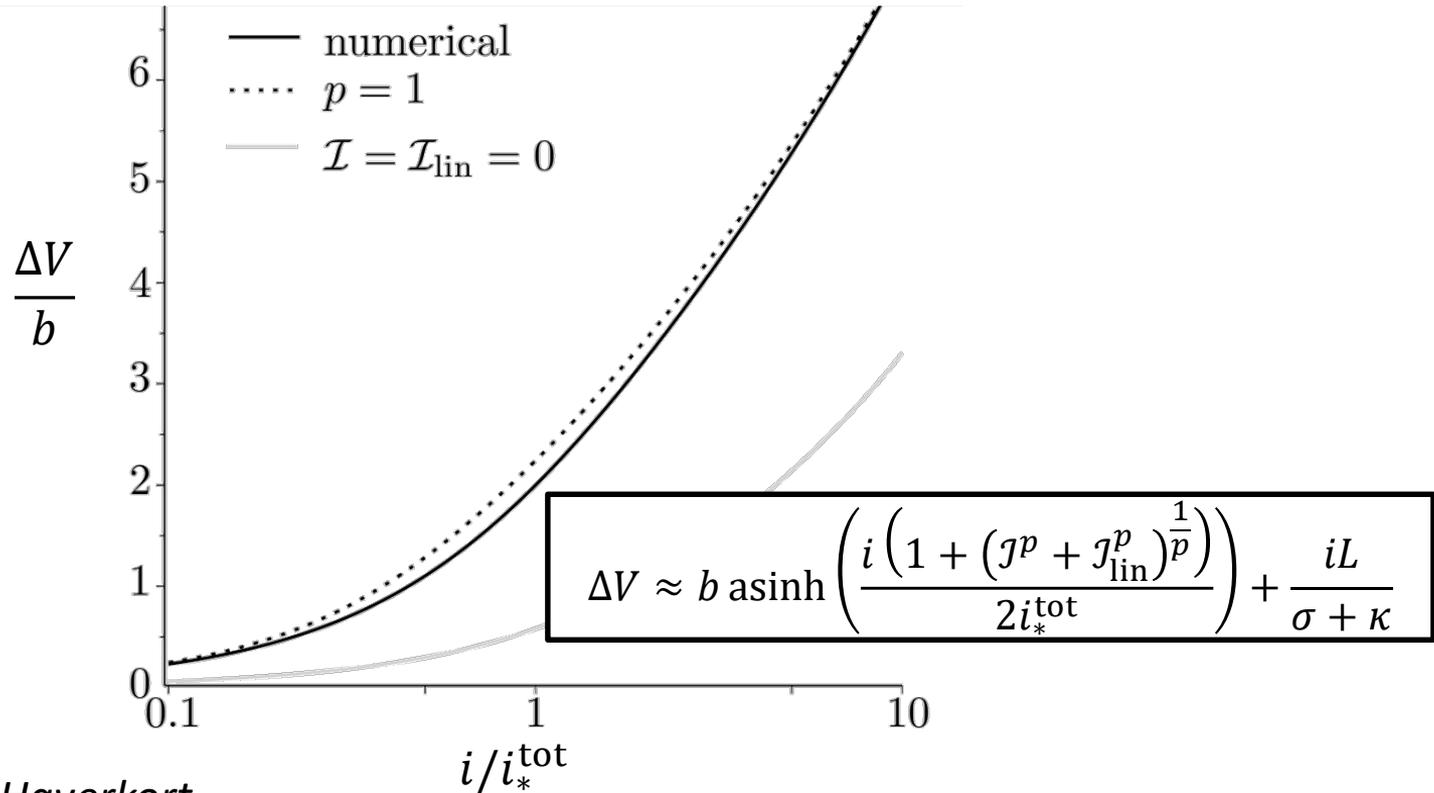
# Optimal porosity

$$\kappa = \kappa_0 \varepsilon^{1.5}, \sigma = \sigma_0 (1 - \varepsilon)^{1.5}$$



$$a = \frac{6(1 - \varepsilon)}{d}$$

# Butler-Volmer kinetics ( $\alpha=1/2$ )



# Conclusions

- Tafel slope  $b(2 - \varepsilon)$
- Thickness  $L_{\text{opt}} \approx \frac{4b\sigma\kappa}{i(\sigma+\kappa)}$  so that  $\frac{1}{3} \leq \varepsilon \leq \frac{2}{3}$
- Accurate *explicit* polarisation equation

Haverkort, J. W. (2019). *Electrochimica Acta*, 295, 846-860.  
*A theoretical analysis of the optimal electrode thickness and porosity.*

[J.W.Haverkort@tudelft.nl](mailto:J.W.Haverkort@tudelft.nl)

[jwhaverkort.weblog.tudelft.nl](http://jwhaverkort.weblog.tudelft.nl)

